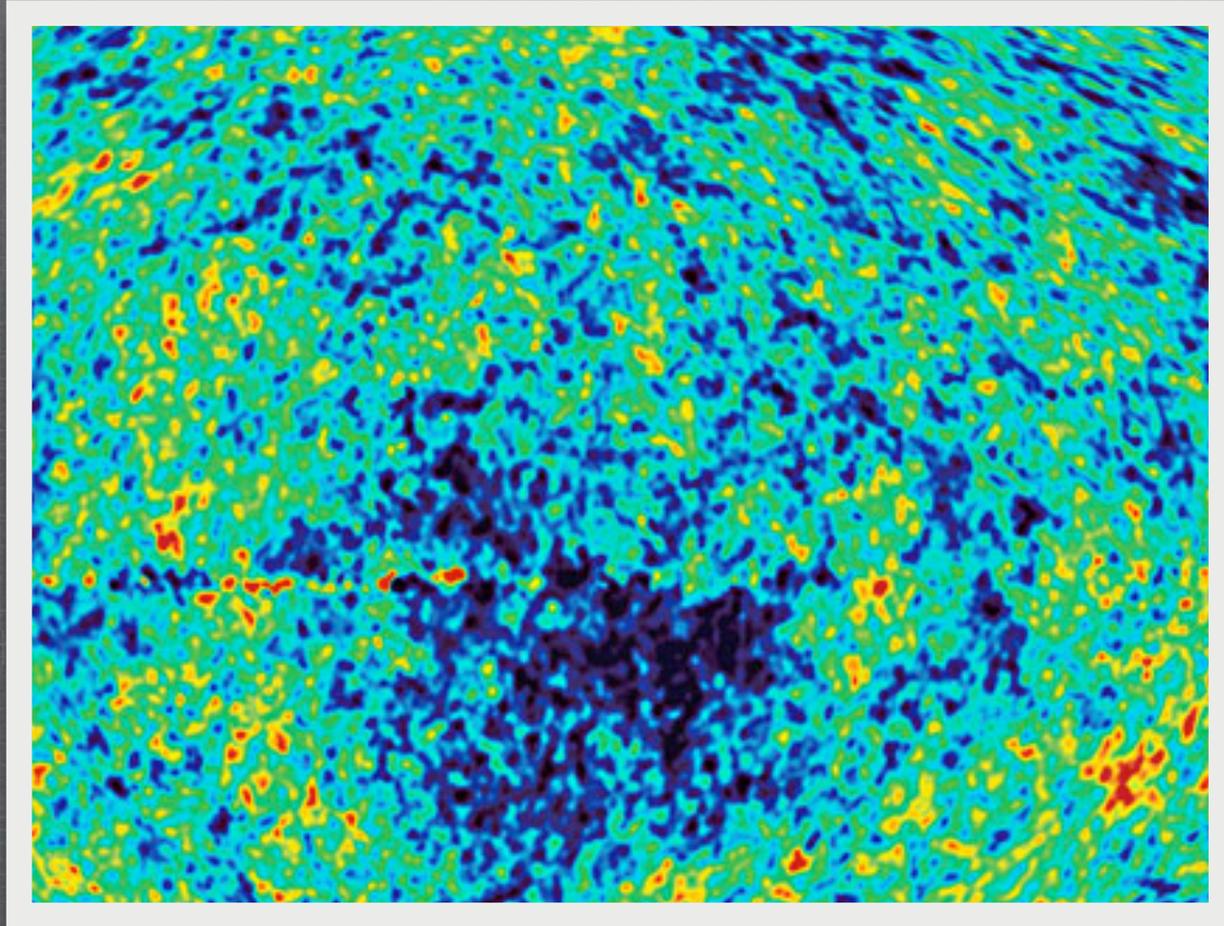


MODELS OF INFLATION



Richard Easther

EVIDENCE!

- Standard hot big bang (BBN, CMB)
 - Dominated by radiation and/or “matter”
 - Universe evolves away from $\Omega = 1$
 - Today: $\Omega = 1.00 \pm .01$
- Homogeneity & Isotropy: CMB: $\delta T/T \sim O(10^{-5})$
- Large scale correlation of CMB E-mode and $\delta T/T$

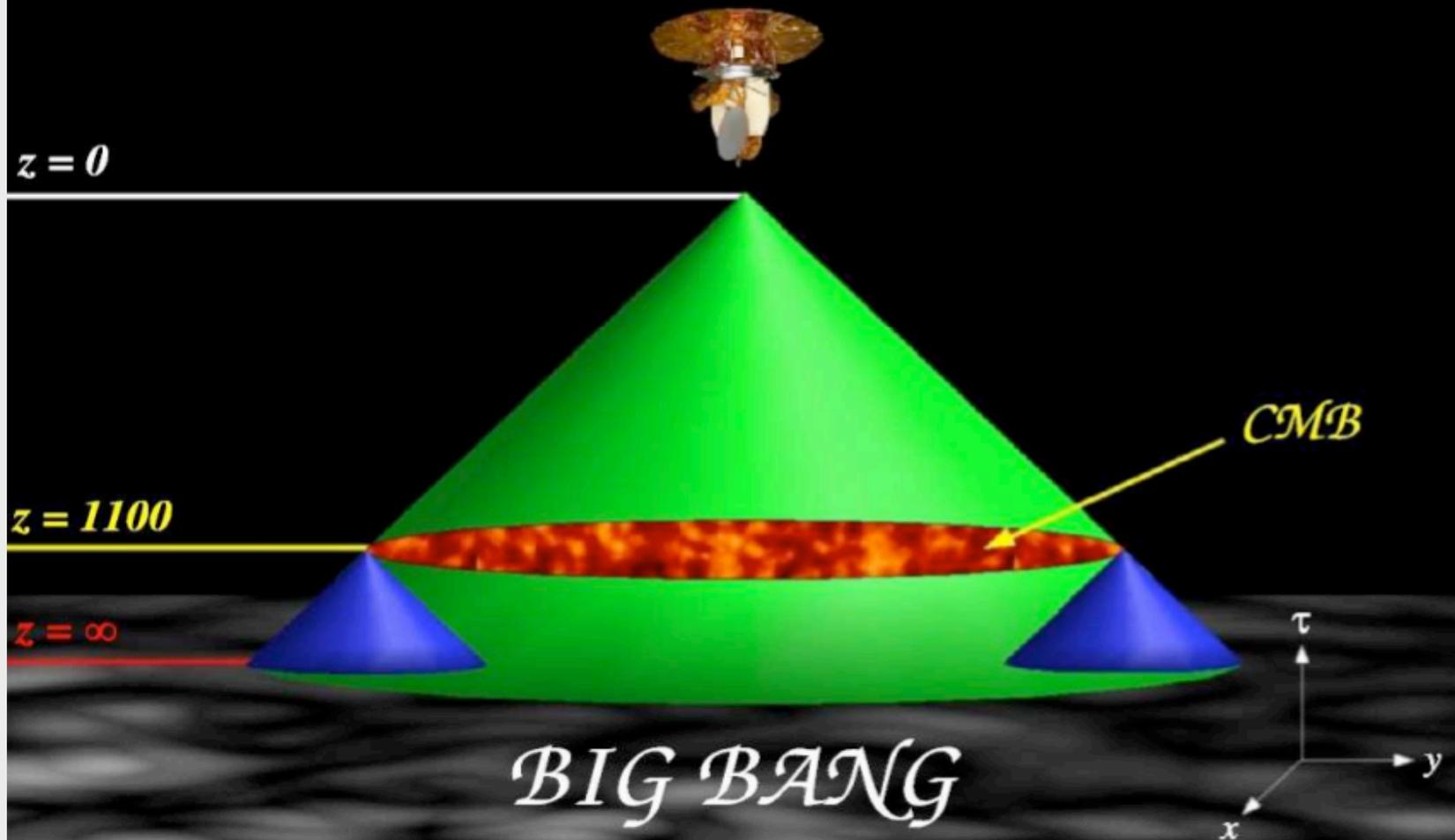
<ET> CORRELATION

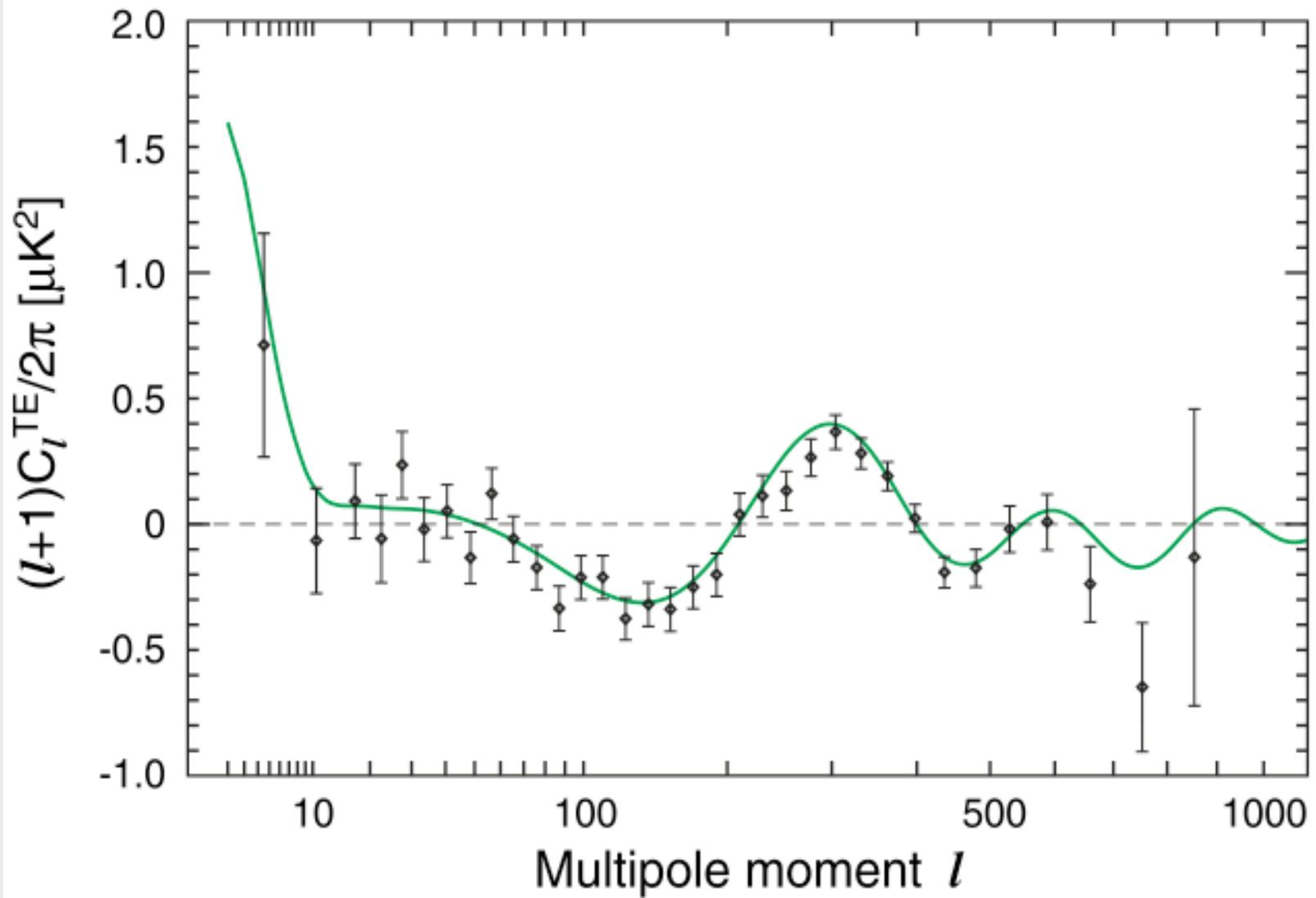
- Physics of the CMB is well understood
 - General relativity and *small* inhomogeneities
 - e^- , p , He nuclei, dark matter, ν , γ , (Λ , H_0 and k)
 - Boltzmann equations
 - Beautiful and largely classical physics

<ET> CORRELATION

- Temperature anisotropies caused by
 - Compression / rarefaction (acoustic peaks)
 - Gravitational redshift (Sachs-Wolfe, ISW)
- *Polarization* (E or B) requires free charges
 - Ionized universe
 - Pre-recombination: $z > 1089$ (or so)
 - Post-reionization: $z < 10$ (or so)

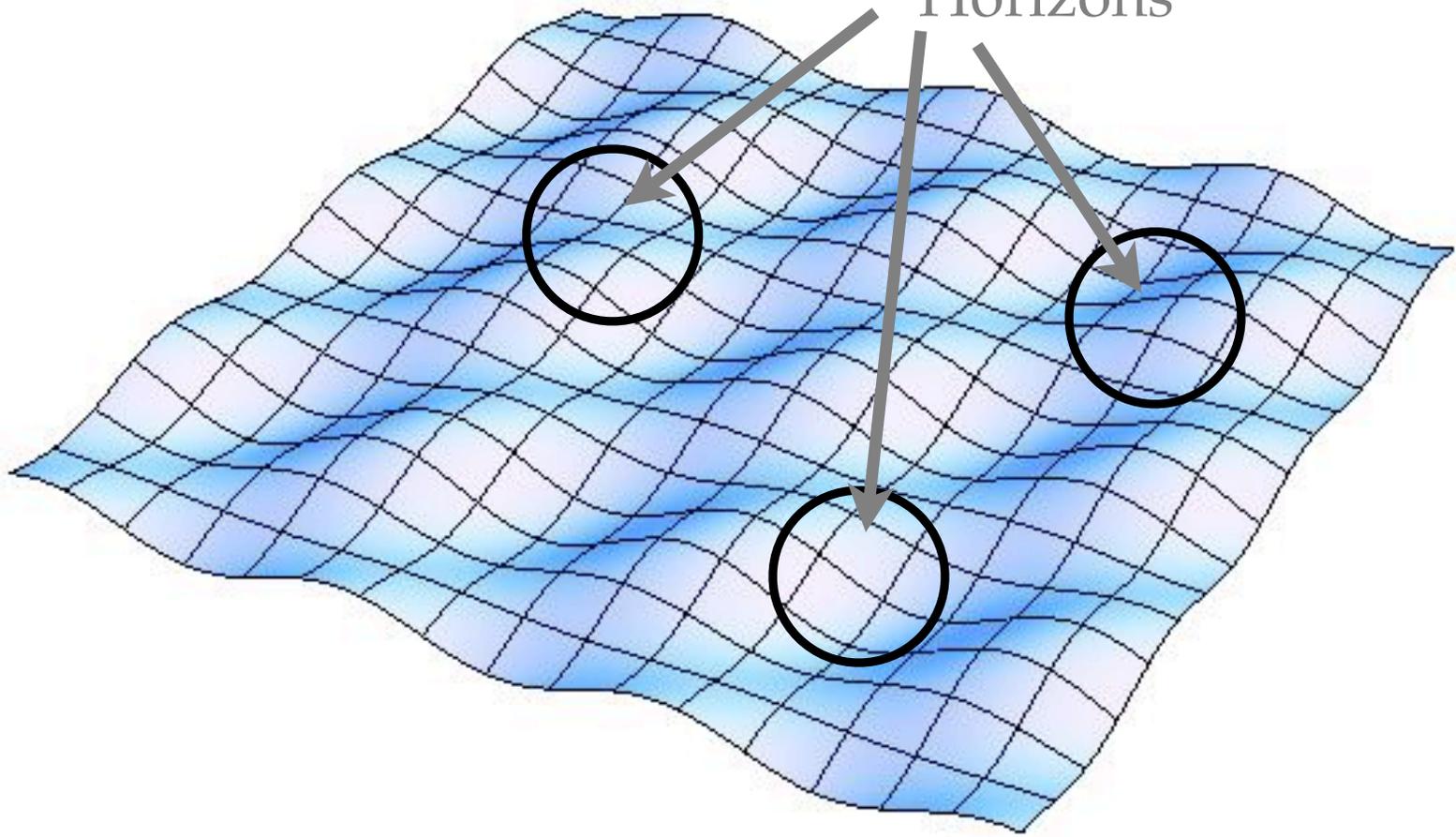
The Horizon Problem

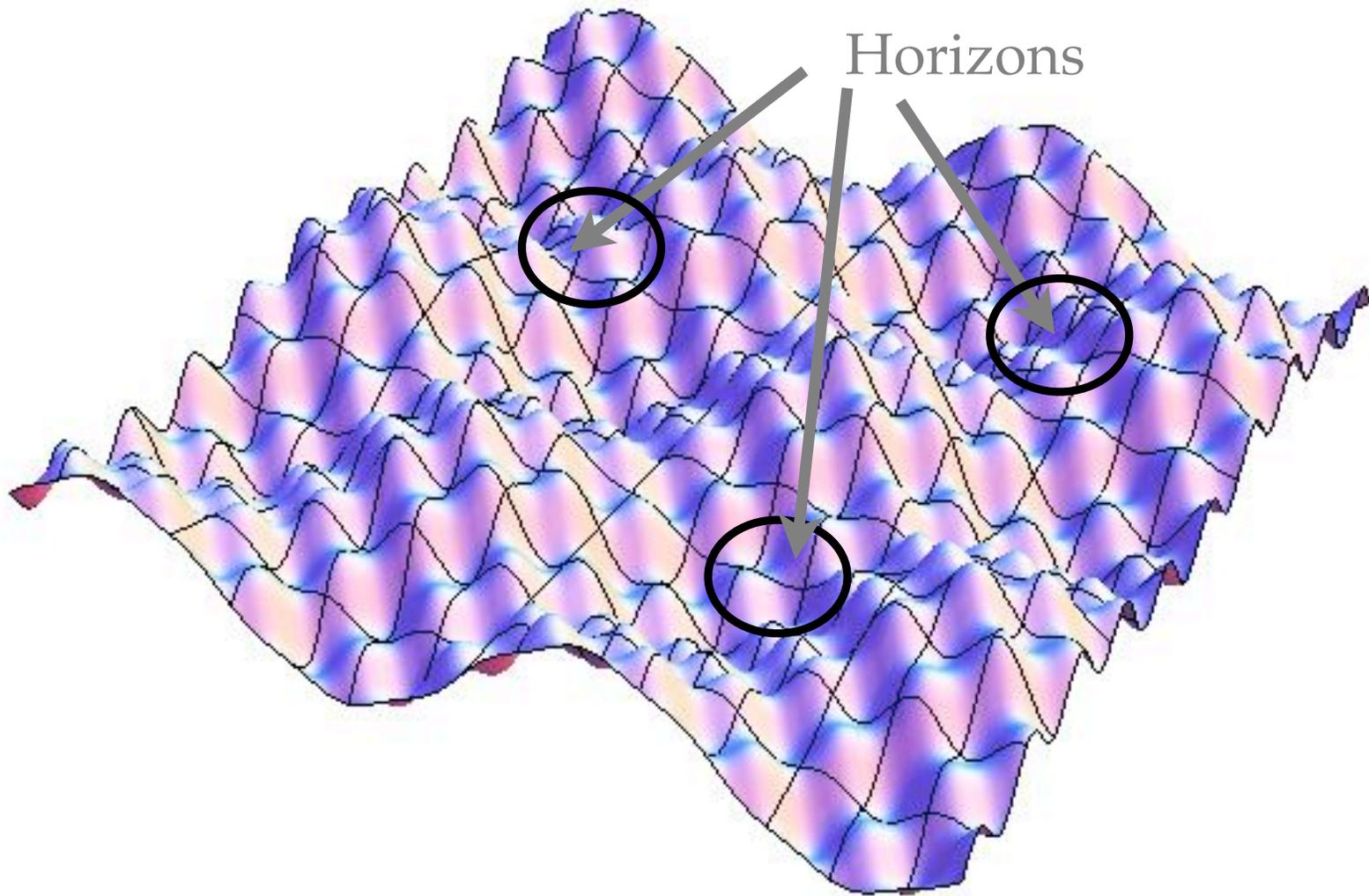




WMAP5

Horizons





Horizons

INFLATION: WORKING DEFINITION #1

- Comoving size of the *horizon* is *decreasing*.
 - Dynamical definition
 - Allows causal theory of initial conditions
 - Explains long range correlations in CMB.
- Standard inflation + Ekpyrosis + “pre big bang” + varying speed of light (see Khoury)

COMMENTARY...

- Amounts to: “inflation is a thing that puts long range correlations in the CMB”
 - We see long range correlations in the CMB
 - Not what we (they) would have expected in 1965!
- Do we conclude inflation happened, and go home?
- We want to know *why* it happened!

INFLATION: WORKING DEFINITION #2

- Expansion of universe is *accelerating*
 - Restricts attention to expanding universe
 - Einstein gravity (after conformal transformation?)
 - “Traditional” definition: but still dynamical
 - No mention yet of *models*

SIMPLE INFLATIONARY MODELS...

- Scalar field
 - Single field
 - Minimally coupled
 - Standard kinetic term.
- Potential $V(\phi)$ specifies model
 - $\exp(\phi)$; $\cos(\phi)$; $m^2\phi^2$; $\lambda\phi^4$ (+ many baroque forms)

WHAT *IS* THE INFLATON?

- Fundamental field in some Beyond the Standard Model theory (must be very weakly interacting)?
- Some dynamical degree of freedom related to branes / compact dimensions?
- A composite or emergent phenomenon involving many individual fields or degrees of freedom?

SCALAR FIELD EVOLUTION

$$\ddot{\phi} + 3H\dot{\phi} + \frac{dV}{d\phi} = 0$$

$$H^2 = \frac{8\pi}{3M_p^2} \rho = \frac{8\pi}{3M_p^2} \left(\frac{\dot{\phi}^2}{2} + V(\phi) \right)$$

SLOW ROLL APPROXIMATION

$$H^2 \approx \frac{8\pi}{3M_p^2} V(\phi) \quad 3H\dot{\phi} + \frac{dV}{d\phi} \approx 0$$

Slow Roll Parameters...

$$\epsilon = \frac{M_p^2}{16\pi} \left(\frac{V'}{V} \right)^2 \quad \eta = \frac{M_p^2}{8\pi} \frac{V''}{V} \quad \dots$$

INFLATIONARY MODELS

- My focus is on general properties
 - Many models (~ 100) of inflation in literature
- Not just functional form of potential
 - e.g. k-inflation / non-minimal kinetic term
 - D-brane / DBI (w. similar considerations about r)
 - Other stringy models / Curvaton / Assisted inflation

SINGLE SCALE FIELD: BASIC FEATURES...

- Need a potential which is very flat
 - Scalar field evolves slowly (“dark energy”)
 - Get slow roll parameters & plug in for predictions
- Have quantum fluctuations
 - In field and in *spacetime* (tensor)
 - Fluctuations in ϕ are fluctuations in $V(\phi)$ (density)

PERTURBATIONS...

- Massless free field has fluctuations of amplitude H
- Inflaton field more complicated
 - Fluctuations gives density perturbations
 - Regions which fluctuate “uphill” need time to roll back to central value
 - $\delta\phi \sim \delta N \sim \delta\rho$
 - $N = \# \text{ of e-folds} = \log(\text{scale factor})$

MOTIVATING δN

- $\delta\phi \sim \delta H$
- Velocity of field from slow roll approximation
- Hubble time $1/H$, $\delta N \sim 1$

$$\begin{aligned}\dot{\phi} &\sim \frac{\delta\phi}{\delta t} \approx \frac{V'(\phi)}{3H} \\ \delta t &\approx \frac{3H\delta\phi}{V'} = \frac{3H^2}{V'} \\ \delta N &\approx \frac{\delta t}{\frac{1}{H}} \sim \frac{H}{M_p} \frac{1}{\sqrt{\epsilon}}\end{aligned}$$

PERTURBATION SPECTRA

$$P_T = 16 \frac{H^2}{M_p^2} = A_T k^{n_t}, \quad n_t = -2\epsilon$$

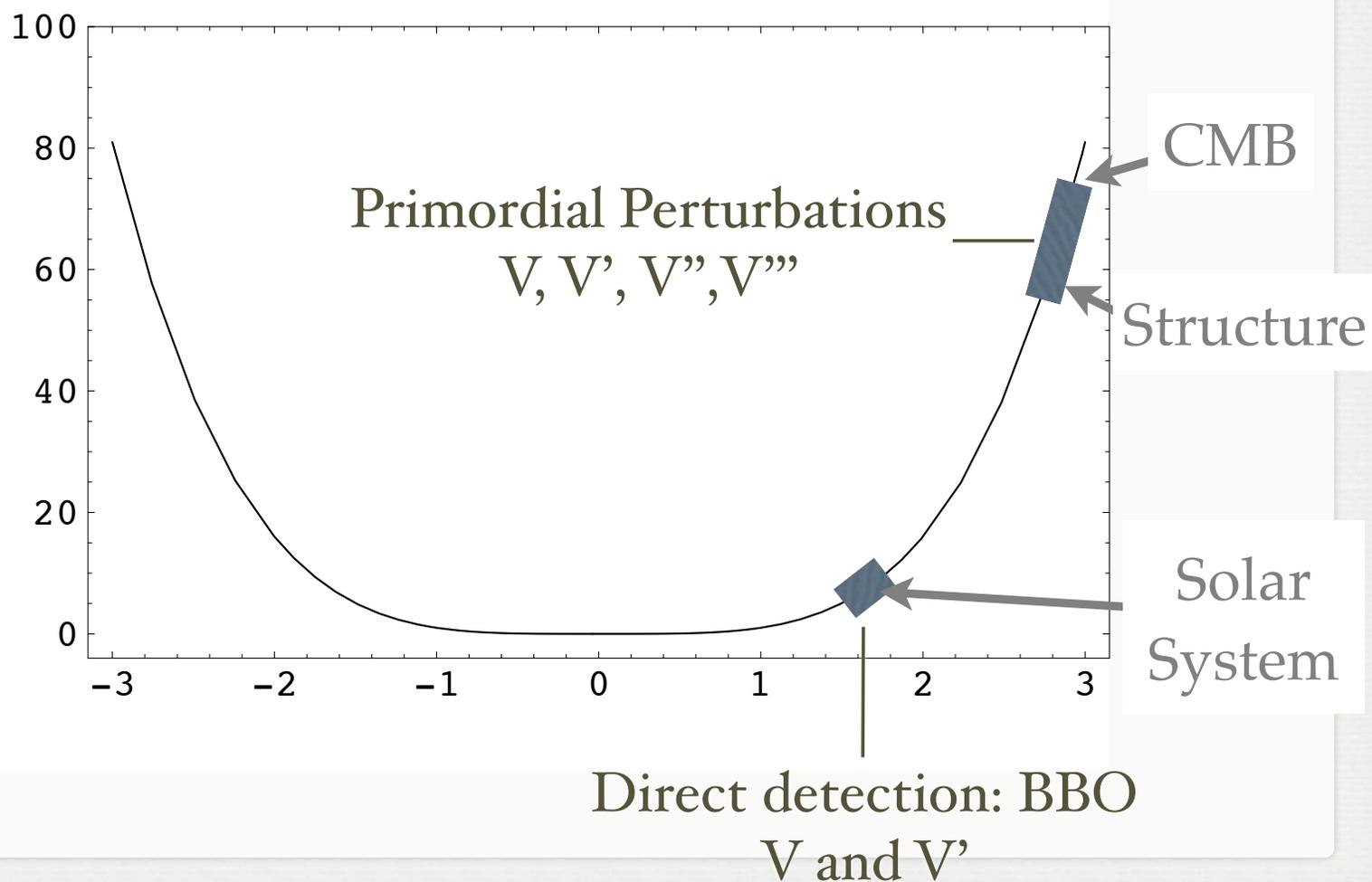
$$P_S = \frac{H^2}{M_p^2 \epsilon} = A_S k^{n_s - 1}, \quad n_s = 1 - 6\epsilon + 2\eta$$

$$\frac{P_T}{P_S} = r = 16\epsilon$$

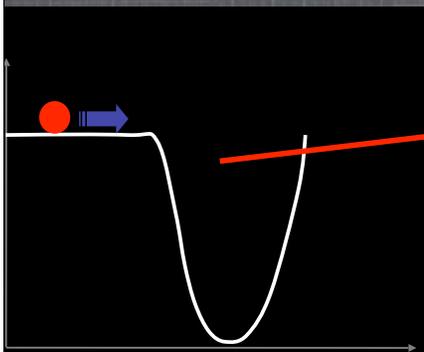
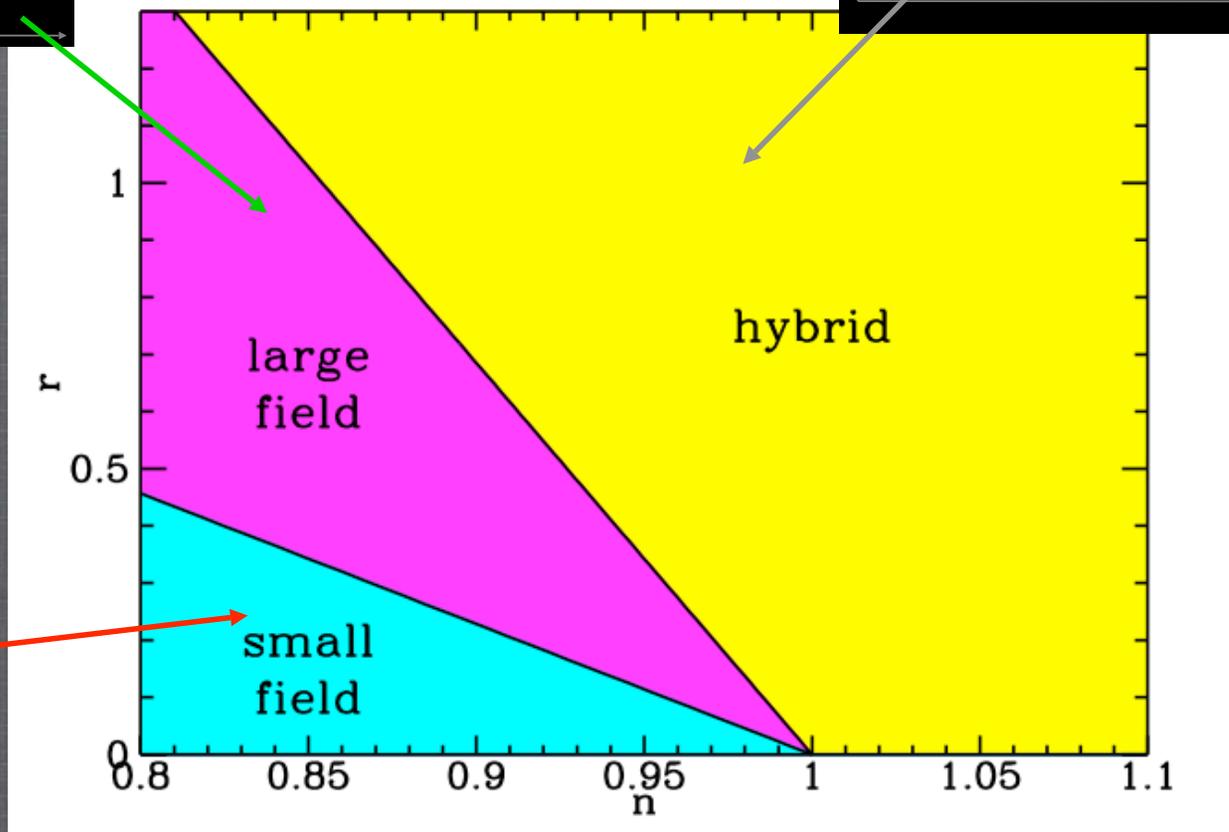
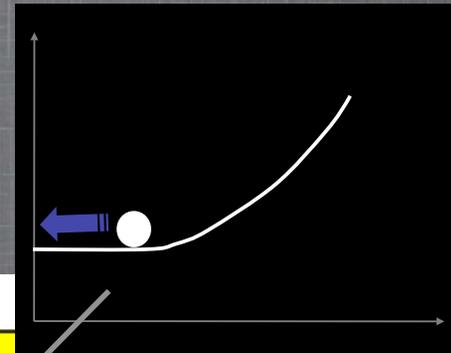
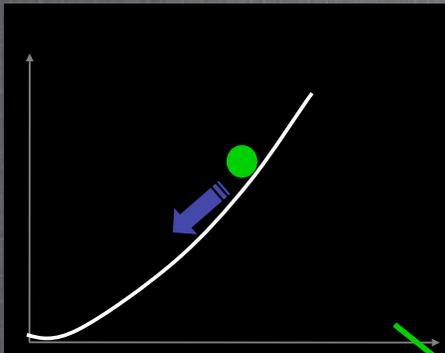
← Consistency Condition

- Indices *change* as field evolves
- Tensors suppressed relative to scalars

CARTOON VERSION...



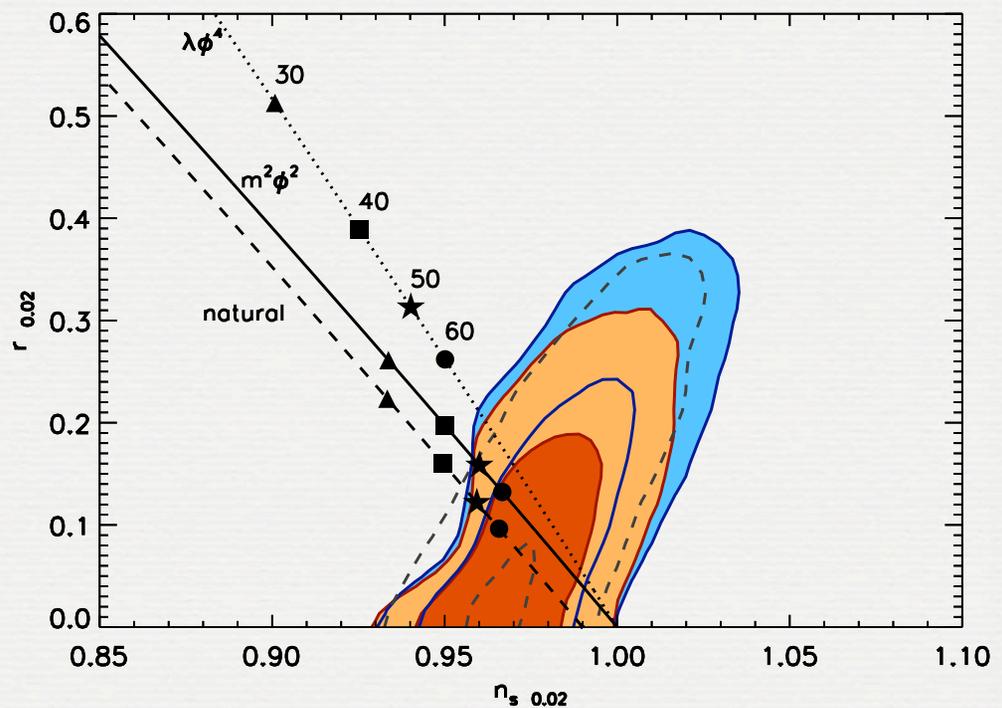
THE INFLATIONARY ZOO



Dodelson and Kinney '97

RECONSTRUCTION...

- Constrain ε and η directly
- w. Peiris, & Adshead
- Better ways of doing slow roll expansion
- Ambiguity in N



PHYSICAL MOTIVATION FOR POTENTIALS

- Very few inflationary models are *derived*
 - e.g. potential *and* parameters extracted from some larger theory (string theory / branes)
- Some are *motivated*
 - e.g. natural inflation - cosine potential from axions
- Many just written down out of thin air...
 - What is normal?

TENSOR AMPLITUDE & “LYTH BOUND”

- Q: How far does field move in an e-fold?

$$\frac{dN}{d\phi} = \frac{dN}{dt} \frac{dt}{d\phi} = H \frac{1}{\frac{d\phi}{dt}}$$

IMPLICATIONS...

- If field moves by more than M_p (for $\Delta N \sim 50$):
 - Do not have perturbative control of potential
 - “Explicit” single field models all have $\delta\phi < M_p$
 - Can write down potentials with $\delta\phi > M_p$
 - But unsure about physical motivation

$$\Delta\phi \sim \Delta N \frac{M_p}{8\sqrt{\pi}} \sqrt{r}$$

EXPECTATIONS FOR TENSORS...

- “Natural” for single field models to have $r \ll 1$??
 - e.g. $r \sim 10^{-6}$ or less
- Experiment: can get to $r \sim 10^{-2}$ from ground?
 - And maybe 10^{-3} or 10^{-4} from space??
- So tensors may be effectively undetectable

IS IT THIS BAD?

- If we look at *algebraically* simple potentials
 - Typically: ε and $\eta \sim 10^{-2}$; $r \sim 0.1$ is “natural”
- $r \sim 10^{-5}$ implies $\varepsilon \sim 10^{-6}$
 - Now *this* looks tuned
- Examples of stringy models; including those with large r : **Kachru and Silverstein**

DESIGN DECISIONS...

- Expectations for tensors are bimodal...
- Either $r \sim 0.01 - 0.2$
 - 2σ detection from ground / balloon / Planck?
- Or $r \sim 10^{-5}$ or less
 - Even a dedicated satellite may not see them!
- Food for thought: How do we respond to each case?

POSSIBLE LEVERS...

- What is the status of the consistency condition?
 - If r is very large can we observe it?
 - How robust is this prediction?
- Can we observe *running* of the spectral index?
 - Not in the CMB alone for “natural” values
- What about the 3-point function?

THOUGHTS

- An experiment that could measure $r \sim 0.001$ would rule out / confirm a *class* of inflationary models
 - A null result would not rule out inflation itself
- Inflation takes us to territory we do not understand
 - GUT scale physics; a probe of string theory?

THANKS TO...

- Peter Adshead, Will Kinney, Eugene Lim, Hiranya Peiris, David Wands